

University of Colorado  
Department of Computer Science  
Chaotic Dynamics – CSCI 4446/5446  
Spring 2012

Problem Set 12

Issued: 10 April 2012

Due: 24 April 2012

Note: only undergraduates are required to turn in this problem set, but *all* students should do the reading listed below.

**Project presentations:** are scheduled during lecture on 24 April and 26 April.

**Reading:** *Classical Mechanics Notes; Berreby paper (will pass out xeroxes).*

**Bibliography:**

- H. Abelson, “The Bifurcation Interpreter: A step towards the automatic analysis of dynamical systems,” *International Journal of Computers and Mathematics with Applications* **20**:13 (1990).
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- M. Hénon and C. Heiles, “The applicability of the third integral of motion: Some numerical experiments,” *Astronomical Journal* **69**:73 (1964)
- M. Hénon, “Numerical exploration of Hamiltonian systems,” in *Chaotic Behaviour of Deterministic Systems*, North-Holland, 1983.
- I. Percival, “Chaos in Hamiltonian systems,” *Proceedings of the Royal Society, London* **413**:131-144 (1987), published in *Dynamical Chaos*, M. Berry, I. Percival, and N. Weiss, eds., University Press, Cambridge UK, 1987. On E-reserves.
- I. Peterson, *Newton’s Clock: Chaos in the Solar System*, Freeman, 1993. On library reserve.
- G. Sussman and J. Wisdom, “Numerical evidence that the motion of Pluto is chaotic,” *Science* **241**:433-437, 1988.
- A. Weigend and N. Gershenfeld, eds., *Time Series Prediction: Forecasting the Future and Understanding the Past*, Santa Fe Institute Studies in the Sciences of Complexity, 1993. On library reserve.

- J. Wisdom, “Chaotic behavior in the solar system,” *Nuclear Physics B* **2**:391-414, 1987.
- J. Wisdom, “Is the solar system stable? and Can we use chaos to make measurements?,” in *Chaos/XAOC : Soviet-American perspectives on nonlinear science*, D. K. Campbell, editor, American Institute of Physics, New York, 1990. On E-reserves.
- K. Yip, *KAM: A System for Intelligently Guiding Numerical Experimentation by Computer*, MIT Press, 1991.
- K. Yip, “Understanding complex dynamics by visual and symbolic reasoning,” *Artificial Intelligence* **51**, Special Volume on Qualitative Reasoning About Physical Systems II, 1991.

### Problems:

Adapt your RK4 algorithm from PS4 to the two-body equations — the system of equations labeled (4) in the *Classical Mechanics Notes*. To do this, you’ll have to pull these equations apart into twelve first-order ODEs by rewriting them out in terms of their coordinates, as I show in the *Notes*.

Plug your answers to problem 4(d) on PS11 into these ODEs and integrate them for half a dozen orbits, using at least 1000 timesteps per orbit period. Plot your results in physical space: one point for each star, looking down from above on the plane of the orbit. Turn in a plot and draw a few arrows to show which way each star is going.

Does your binary orbit properly? Does the center of mass appear to move? Which way?