# Representation Learning 

Natural Language Processing: Jordan<br>Boyd-Graber<br>University of Maryland<br>UPDATE EXAMPLES

## Dataset

- Two types of words
- Vehicles
- Fruits
- Learn a representation with two dimensions
- Word2Vec skipgram negative sampling
- $\alpha=1.0$ (bad choice in practice!)
- We'll do update for one positive and one negative sample
- Note: much of word2vec magic is sampling negative words, you'll have to take my word for it


## Word

| ambulance | -0.228 | 0.099 |
| :--- | :---: | :---: |
| apple | 0.078 | 0.217 |
| backhoe | -0.086 | 0.138 |
| banana | 0.046 | 0.195 |
| crane | -0.220 | 0.153 |
| firetruck | 0.039 | -0.047 |
| lemon | 0.008 | -0.043 |
| strawberry | 0.202 | -0.081 |

$$
\begin{align*}
z & =w_{\text {focus }}^{\top} \cdot c_{s}  \tag{1}\\
E_{s} & = \begin{cases}1-\sigma(z), & \text { if } s \text { postive example } \\
0-\sigma(z), & \text { if } s \text { negative example }\end{cases}  \tag{2}\\
\Delta \vec{w}_{\text {focus }} & =\alpha E_{s} \vec{c}_{s}  \tag{3}\\
\Delta \vec{c}_{s} & =\alpha E_{s} \vec{w}_{\text {focus }} \tag{4}
\end{align*}
$$

$$
\alpha=0.1
$$

## POS (focus: banana, sample: lemon)

POS (focus: banana, sample: lemon)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {lemon }}$


## POS (focus: banana, sample: lemon)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {lemon }}=0.046 * 0.000+0.195 * 0.000$


## POS (focus: banana, sample: lemon)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {lemon }}=0.046 * 0.000+0.195 * 0.000=0.000$


## POS (focus: banana, sample: lemon)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {lemon }}=0.046 * 0.000+0.195 * 0.000=0.000$
- $e=1.0-\pi=1.0-\sigma(0.000)=$


## POS (focus: banana, sample: lemon)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {lemon }}=0.046 * 0.000+0.195 * 0.000=0.000$
- $e=1.0-\pi=1.0-\sigma(0.000)=0.500$

POS (focus: banana, sample: lemon)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {lemon }}=0.046 * 0.000+0.195 * 0.000=0.000$
- $e=1.0-\pi=1.0-\sigma(0.000)=0.500$
- $\Delta w_{\text {banana }}=\alpha e \cdot c_{\text {lemon }}=$

POS (focus: banana, sample: lemon)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {lemon }}=0.046 * 0.000+0.195 * 0.000=0.000$
- $e=1.0-\pi=1.0-\sigma(0.000)=0.500$
- $\Delta w_{\text {banana }}=\alpha e \cdot c_{\text {lemon }}=0.10 \cdot 0.500 \cdot(0.000,0.000)=$

POS (focus: banana, sample: lemon)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {lemon }}=0.046 * 0.000+0.195 * 0.000=0.000$
- $e=1.0-\pi=1.0-\sigma(0.000)=0.500$
- $\Delta w_{\text {banana }}=\alpha e \cdot c_{\text {lemon }}=0.10 \cdot 0.500 \cdot(0.000,0.000)=(0.000,0.000)$

POS (focus: banana, sample: lemon)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {lemon }}=0.046 * 0.000+0.195 * 0.000=0.000$
- $e=1.0-\pi=1.0-\sigma(0.000)=0.500$
- $\Delta w_{\text {banana }}=\alpha e \cdot c_{\text {lemon }}=0.10 \cdot 0.500 \cdot(0.000,0.000)=(0.000,0.000)$
- $\Delta c_{\text {lemon }}=\alpha e \cdot m_{\text {banana }}=$

POS (focus: banana, sample: lemon)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {lemon }}=0.046 * 0.000+0.195 * 0.000=0.000$
- $e=1.0-\pi=1.0-\sigma(0.000)=0.500$
- $\Delta w_{\text {banana }}=\alpha e \cdot c_{\text {lemon }}=0.10 \cdot 0.500 \cdot(0.000,0.000)=(0.000,0.000)$
- $\Delta c_{\text {lemon }}=\alpha e \cdot m_{\text {banana }}=0.10 \cdot 0.500 \cdot(0.046,0.195)=$

POS (focus: banana, sample: lemon)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {lemon }}=0.046 * 0.000+0.195 * 0.000=0.000$
- $e=1.0-\pi=1.0-\sigma(0.000)=0.500$
- $\Delta w_{\text {banana }}=\alpha e \cdot c_{\text {lemon }}=0.10 \cdot 0.500 \cdot(0.000,0.000)=(0.000,0.000)$
- $\Delta c_{\text {lemon }}=\alpha e \cdot m_{\text {banana }}=0.10 \cdot 0.500 \cdot(0.046,0.195)=(0.002,0.010)$

NEG (focus: banana, sample: firetruck)

- $z=w_{\text {banana }}^{\top} \cdot C_{\text {firetruck }}$

NEG (focus: banana, sample: firetruck)

- $z=w_{\text {banana }}^{\top} \cdot C_{\text {firetruck }}=0.046 * 0.000+0.195 * 0.000$

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NEG (focus: banana, sample: firetruck)

- $z=w_{\text {banana }}^{\top} \cdot C_{\text {firetruck }}=0.046 * 0.000+0.195 * 0.000=0.000$
- $e=0.0-\pi=0.0-\sigma(0.000)=-0.500$

NEG (focus: banana, sample: firetruck)

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- $\Delta w_{\text {banana }}=\alpha e \cdot c_{\text {firetruck }}=$

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- $\Delta w_{\text {banana }}=\alpha e \cdot c_{\text {firetruck }}=0.10 \cdot-0.500 \cdot(0.000,0.000)=$

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- $\Delta w_{\text {banana }}=\alpha e \cdot c_{\text {firetruck }}=0.10 \cdot-0.500 \cdot(0.000,0.000)=$ (-0.000,-0.000)

NEG (focus: banana, sample: firetruck)

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- $e=0.0-\pi=0.0-\sigma(0.000)=-0.500$
- $\Delta w_{\text {banana }}=\alpha e \cdot c_{\text {firetruck }}=0.10 \cdot-0.500 \cdot(0.000,0.000)=$ (-0.000,-0.000)
- $\Delta c_{\text {firetruck }}=\alpha e \cdot w_{\text {banana }}=$

NEG (focus: banana, sample: firetruck)

- $z=w_{\text {banana }}^{\top} \cdot c_{\text {firetruck }}=0.046 * 0.000+0.195 * 0.000=0.000$
- $e=0.0-\pi=0.0-\sigma(0.000)=-0.500$
- $\Delta w_{\text {banana }}=\alpha e \cdot c_{\text {firetruck }}=0.10 \cdot-0.500 \cdot(0.000,0.000)=$ (-0.000,-0.000)
- $\Delta c_{\text {firetruck }}=\alpha e \cdot w_{\text {banana }}=0.10 \cdot-0.500 \cdot(0.046,0.195)=$

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- $\Delta c_{\text {firetruck }}=\alpha e \cdot w_{\text {banana }}=0.10 \cdot-0.500 \cdot(0.046,0.195)=$ (-0.002,-0.010)

| Word |  |  |
| :--- | :---: | :---: |
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| strawberry | 0.202 | -0.081 |

$$
\alpha=0.1
$$

## Much later ...

## Vectors are starting to take shape

## Word

| ambulance | -0.906 | 0.107 |
| :--- | :---: | :---: |
| apple | 0.992 | 0.780 |
| backhoe | -0.902 | 0.459 |
| banana | 1.286 | 0.573 |
| crane | -1.119 | 0.399 |
| firetruck | -0.830 | 0.094 |
| lemon | 0.750 | -0.289 |
| strawberry | 1.174 | -0.379 |

## Context

| ambulance | -0.927 | -0.090 |
| :--- | :---: | :---: |
| apple | 0.973 | -0.923 |
| backhoe | -0.984 | -0.379 |
| banana | 0.634 | -0.486 |
| crane | -1.258 | -0.188 |
| firetruck | -1.224 | -0.060 |
| lemon | 1.087 | -0.081 |
| strawberry | 1.054 | 0.410 |

$$
\begin{align*}
z & =w_{\text {focus }}^{\top} \cdot c_{s}  \tag{5}\\
E_{s} & = \begin{cases}1-\sigma(z), & \text { if } s \text { postive example } \\
0-\sigma(z), & \text { if } s \text { negative example }\end{cases}  \tag{6}\\
\Delta \vec{w}_{\text {focus }} & =\alpha E_{s} \vec{c}_{s}  \tag{7}\\
\Delta \vec{c}_{s} & =\alpha E_{s} \vec{w}_{\text {focus }} \tag{8}
\end{align*}
$$

$$
\alpha=0.1
$$

## POS (focus: firetruck, sample: backhoe)

- $z=w_{\text {firetruck }}^{\top} \cdot C_{\text {backhoe }}$

POS (focus: firetruck, sample: backhoe)

- $z=w_{\text {firetruck }}^{\top} \cdot C_{\text {backhoe }}=-0.830 *-0.984+0.094 *-0.379$

POS (focus: firetruck, sample: backhoe)

- $z=w_{\text {firetruck }}^{\top} \cdot C_{\text {backhoe }}=-0.830 *-0.984+0.094 *-0.379=0.780$


## POS (focus: firetruck, sample: backhoe)

- $z=w_{\text {firetruck }}^{\top} \cdot C_{\text {backhoe }}=-0.830 *-0.984+0.094 *-0.379=0.780$
- $e=1.0-\pi=1.0-\sigma(0.780)=$


## POS (focus: firetruck, sample: backhoe)

- $z=w_{\text {firetruck }}^{\top} \cdot C_{\text {backhoe }}=-0.830 *-0.984+0.094 *-0.379=0.780$
- $e=1.0-\pi=1.0-\sigma(0.780)=0.314$

POS (focus: firetruck, sample: backhoe)

- $z=w_{\text {firetruck }}^{\top} \cdot C_{\text {backhoe }}=-0.830 *-0.984+0.094 *-0.379=0.780$
- $e=1.0-\pi=1.0-\sigma(0.780)=0.314$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {backhoe }}=$

POS (focus: firetruck, sample: backhoe)

- $z=w_{\text {firetruck }}^{\top} \cdot C_{\text {backhoe }}=-0.830 *-0.984+0.094 *-0.379=0.780$
- $e=1.0-\pi=1.0-\sigma(0.780)=0.314$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {backhoe }}=0.10 \cdot 0.314 \cdot(-0.984,-0.379)=$


## POS (focus: firetruck, sample: backhoe)

- $z=w_{\text {firetruck }}^{\top} \cdot C_{\text {backhoe }}=-0.830 *-0.984+0.094 *-0.379=0.780$
- $e=1.0-\pi=1.0-\sigma(0.780)=0.314$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {backhoe }}=0.10 \cdot 0.314 \cdot(-0.984,-0.379)=$ (-0.031,-0.012)

POS (focus: firetruck, sample: backhoe)

- $z=w_{\text {firetruck }}^{\top} \cdot C_{\text {backhoe }}=-0.830 *-0.984+0.094 *-0.379=0.780$
- $e=1.0-\pi=1.0-\sigma(0.780)=0.314$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {backhoe }}=0.10 \cdot 0.314 \cdot(-0.984,-0.379)=$ (-0.031,-0.012)
- $\Delta c_{\text {backhoe }}=\alpha e \cdot w_{\text {firetruck }}=$

POS (focus: firetruck, sample: backhoe)

- $z=w_{\text {firetruck }}^{\top} \cdot C_{\text {backhoe }}=-0.830 *-0.984+0.094 *-0.379=0.780$
- $e=1.0-\pi=1.0-\sigma(0.780)=0.314$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {backhoe }}=0.10 \cdot 0.314 \cdot(-0.984,-0.379)=$ (-0.031,-0.012)
- $\Delta c_{\text {backhoe }}=\alpha e \cdot w_{\text {firetruck }}=0.10 \cdot 0.314 \cdot(-0.830,0.094)=$

POS (focus: firetruck, sample: backhoe)

- $z=w_{\text {firetruck }}^{\top} \cdot C_{\text {backhoe }}=-0.830 *-0.984+0.094 *-0.379=0.780$
- $e=1.0-\pi=1.0-\sigma(0.780)=0.314$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {backhoe }}=0.10 \cdot 0.314 \cdot(-0.984,-0.379)=$ (-0.031,-0.012)
- $\Delta c_{\text {backhoe }}=\alpha e \cdot w_{\text {firetruck }}=0.10 \cdot 0.314 \cdot(-0.830,0.094)=$ (-0.026, 0.003)

NEG (focus: firetruck, sample: crane)

- $z=w_{\text {firetruck }}^{\top} \cdot c_{\text {crane }}$

NEG (focus: firetruck, sample: crane)

- $z=w_{\text {firetruck }}^{\top} \cdot c_{\text {crane }}=-0.830 *-1.258+0.094 *-0.188$

NEG (focus: firetruck, sample: crane)

- $z=w_{\text {firetruck }}^{\top} \cdot c_{\text {crane }}=-0.830 *-1.258+0.094 *-0.188=1.025$

NEG (focus: firetruck, sample: crane)

- $z=w_{\text {firetruck }}^{\top} \cdot c_{\text {crane }}=-0.830 *-1.258+0.094 *-0.188=1.025$
- $e=0.0-\pi=0.0-\sigma(1.025)=$

NEG (focus: firetruck, sample: crane)

- $z=w_{\text {firetruck }}^{\top} \cdot c_{\text {crane }}=-0.830 *-1.258+0.094 *-0.188=1.025$
- $e=0.0-\pi=0.0-\sigma(1.025)=-0.736$

NEG (focus: firetruck, sample: crane)

- $z=w_{\text {firetruck }}^{\top} \cdot c_{\text {crane }}=-0.830 *-1.258+0.094 *-0.188=1.025$
- $e=0.0-\pi=0.0-\sigma(1.025)=-0.736$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {crane }}=$

NEG (focus: firetruck, sample: crane)

- $z=w_{\text {firetruck }}^{\top} \cdot c_{\text {crane }}=-0.830 *-1.258+0.094 *-0.188=1.025$
- $e=0.0-\pi=0.0-\sigma(1.025)=-0.736$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {crane }}=0.10 \cdot-0.736 \cdot(-1.258,-0.188)=$

NEG (focus: firetruck, sample: crane)

- $z=w_{\text {firetruck }}^{\top} \cdot c_{\text {crane }}=-0.830 *-1.258+0.094 *-0.188=1.025$
- $e=0.0-\pi=0.0-\sigma(1.025)=-0.736$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {crane }}=0.10 \cdot-0.736 \cdot(-1.258,-0.188)=$ (0.093, 0.014)

NEG (focus: firetruck, sample: crane)

- $z=w_{\text {firetruck }}^{\top} \cdot c_{\text {crane }}=-0.830 *-1.258+0.094 *-0.188=1.025$
- $e=0.0-\pi=0.0-\sigma(1.025)=-0.736$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {crane }}=0.10 \cdot-0.736 \cdot(-1.258,-0.188)=$ (0.093, 0.014)
- $\Delta c_{\text {crane }}=\alpha e \cdot w_{\text {firetruck }}=$

NEG (focus: firetruck, sample: crane)

- $z=w_{\text {firetruck }}^{\top} \cdot c_{\text {crane }}=-0.830 *-1.258+0.094 *-0.188=1.025$
- $e=0.0-\pi=0.0-\sigma(1.025)=-0.736$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {crane }}=0.10 \cdot-0.736 \cdot(-1.258,-0.188)=$ (0.093, 0.014)
- $\Delta c_{\text {crane }}=\alpha e \cdot w_{\text {firetruck }}=0.10 \cdot-0.736 \cdot(-0.830,0.094)=$

NEG (focus: firetruck, sample: crane)

- $z=w_{\text {firetruck }}^{\top} \cdot c_{\text {crane }}=-0.830 *-1.258+0.094 *-0.188=1.025$
- $e=0.0-\pi=0.0-\sigma(1.025)=-0.736$
- $\Delta w_{\text {firetruck }}=\alpha e \cdot c_{\text {crane }}=0.10 \cdot-0.736 \cdot(-1.258,-0.188)=$ (0.093, 0.014)
- $\Delta c_{\text {crane }}=\alpha e \cdot w_{\text {firetruck }}=0.10 \cdot-0.736 \cdot(-0.830,0.094)=$ (0.061,-0.007)

| Word |  |  |
| :--- | :---: | :---: |
| ambulance | -0.906 | 0.107 |
| apple | 0.992 | 0.780 |
| backhoe | -0.902 | 0.459 |
| banana | 1.286 | 0.573 |
| crane | -1.119 | 0.399 |
| firetruck | -0.833 | 0.086 |
| lemon | 0.750 | -0.289 |
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$$
\alpha=0.1
$$

## Word Vectors



## Context Vectors



